

Appendix B: Statistical Analysis of Bede's Use of Clausulae

Table 6: *Cursus mixtus* and metrical forms in Bede

A = planus, B = tardus, C = velox, D = trispondaicus, E = medius, F = dispondaicus, G = other

Table 7: Metrical forms in Bede and Oberhelman's control authors¹

H = Bede, I = Descartes, J = Polydore, K = Cicero, L = Dante, M = Gilbert, N = John of Salisbury.

¹ Data taken from Oberhelman, *Rhetoric and Homiletics*, Table I.

Table 8: cursus mixtus forms in Bede and Oberhelman's control authors²

	planus	tardus	velox	trispond.	medius	dispond.	other	total
Bede	135	85	20	35	72	8	12	367
Descartes	293	117	130	213	68	144	35	1000
Polydore	296	119	96	203	132	100	54	1000
Cicero	276	136	133	236	99	85	35	1000
Dante	93	50	93	0	2	10	0	248
Gilbert	210	141	142	133	31	27	23	707
John	84	259	356	153	45	37	23	1260

Equation 1Confidence interval for single proportion:³

$$P_L = \frac{(2np + c_{\alpha/2}^2 - 1) - c_{\alpha/2} \sqrt{c_{\alpha/2}^2 - (2 + 1/n) + 4p(nq + 1)}}{2(n + c_{\alpha/2}^2)}$$

$$P_U = \frac{(2np + c_{\alpha/2}^2 + 1) + c_{\alpha/2} \sqrt{c_{\alpha/2}^2 + (2 + 1/n) + 4p(nq + 1)}}{2(n + c_{\alpha/2}^2)}$$

Where n is the total (so 367 for Bede), p is the proportion of the relevant result ($240/367 = 0.653$), where $c_{\alpha/2} = 2.75$,⁴ where $q = n - p$. P_L and P_U give us the upper and lower limits of the confidence interval, and we have a 99% confidence that the values lie between these two limits.

Table 9: 99% confidence interval on planus, tardus and velox forms in Descartes, Polydore and Cicero:^{*}
. cii 3000 1596, level (99)

-- Binomial Exact --				
Variable	Obs	Mean	Std. Err.	[99% Conf. Interval]
3000	.532	.00911	.5083315	.5555661

² Data taken from Oberhelman, *Rhetoric and Homiletics*, Table I.³ J. L. Fleiss, *Statistical Methods for Rates and Proportions*, 2nd edn (New York, 1981)⁴ This is the cut-off point in the normal distribution.

* The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The output from the program has been copied into this appendix. The first line is the relevant command.

Table 10: 99% confidence interval on *planus*, *tardus* and *velox* forms in Dante, Gilbert and John:^{*}
. cii 1260 1002, level (99)

Variable	Obs	Mean	Std. Err.	[99% Conf. Interval]
1260	.7952381	.0113681	.7644597	.8237501

Table 11: 99% confidence interval on *trispondaicus* forms in Descartes, Polydore and Cicero:^{*}
. cii 3000 652, level (99)

Variable	Obs	Mean	Std. Err.	[99% Conf. Interval]
3000	.2173333	.0075299	.1982337	.2373393

Table 12: 99% confidence interval on *trispondaicus* forms in Dante and John:^{*}
. cii 553 20, level (99)

Variable	Obs	Mean	Std. Err.	[99% Conf. Interval]
553	.0361664	.0079395	.0188705	.0618595

Table 13: 99% confidence interval on *trispondaicus* forms in Gilbert:^{*}
. cii 707 133, level (99)

Variable	Obs	Mean	Std. Err.	[99% Conf. Interval]
707	.1881188	.0146978	.1517713	.2287556

Table 14: 99% confidence interval on metrical forms in Descartes and Polydore:^{*}
. cii 2000 1379, level (99)

Variable	Obs	Mean	Std. Err.	[99% Conf. Interval]
2000	.6895	.0103462	.6621677	.7159203

* The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

Table 15: 99% confidence interval on metrical forms in Cicero:^{*}
. cii 1000 781, level (99)

Variable	Obs	Mean	Std. Err. [99% Conf. Interval]
1000	.781	.0130782	.7455039 .8137749

Table 16: 99% confidence interval on metrical forms in Dante and John:^{*}
cii 553 429, level (99)

Variable	Obs	Mean	Std. Err. [99% Conf. Interval]
553	.7757685	.0177358	.7268847 .819801

Table 17: 99% confidence interval on metrical forms in Gilbert:^{*}
. cii 707 552, level (99)

Variable	Obs	Mean	Std. Err. [99% Conf. Interval]
707	.7807638	.0155599	.7381366 .8195347

Equation 2

In my analyses, I used the upper value produced by the calculation of the confidence interval to produce the expected frequencies, by multiplying the upper limit by the total number of controls (so $0.555 \times 3000 = 1665$), then used this figure in the test below:

$$\chi^2 \text{ test:}^5 \chi^2_{obt} = \sum \frac{(f_o - f_e)^2}{f_e}$$

where f_o = observed frequency and f_e = expected frequency and χ^2_{obt} = the result obtained.

^{*} The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

⁵ Pagano, *Understanding Statistics*, p. 403.

Table 18: χ^2 test on *planus*, *tardus* and *velox* forms in Descartes, Polydore and Cicero against Bede:^{*}

```
. tabi 1665 240 \1335 127, chi2 expec
```

Key			
frequency	expected frequency		
col			
row	1	2	Total
1	1,665	240	1,905
	1,697.4	207.6	1,905.0
2	1,335	127	1,462
	1,302.6	159.4	1,462.0
Total	3,000	367	3,367
	3,000.0	367.0	3,367.0

Pearson chi2(1) = 13.0325 Pr = 0.000

Table 19: χ^2 test on *planus*, *tardus* and *velox* forms in Dante, Gilbert and John against Bede:^{*}

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. tabi 1037 240 \223 127, chi2 expec
```

Key			
frequency	expected frequency		
col			
row	1	2	Total
1	1,037	240	1,277
	988.9	288.1	1,277.0
2	223	127	350
	271.1	78.9	350.0
Total	1,260	367	1,627
	1,260.0	367.0	1,627.0

Pearson chi2(1) = 48.1141 Pr = 0.000

* The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

Table 20: χ^2 test on *trispondaicus* forms in Descartes, Polydore and Cicero against Bede:^{*}

```
. tabi 711 72 \2289 295, chi2 expec
```

Key			
frequency	expected frequency		
col			
row	1	2	Total
1	711	72	783
	697.7	85.3	783.0
2	2,289	295	2,584
	2,302.3	281.7	2,584.0
Total	3,000	367	3,367
	3,000.0	367.0	3,367.0

Pearson chi2(1) = 3.0522 Pr = 0.081

0.081×5 = 0.405 P> α

Table 21: χ^2 test on *trispondaicus* forms in Dante and John against Bede:^{*}

```
. tabi 34 72 \515 295, chi2 expec
```

Key			
frequency	expected frequency		
col			
row	1	2	Total
1	34	72	106
	63.7	42.3	106.0
2	519	295	814
	489.3	324.7	814.0
Total	553	367	920
	553.0	367.0	920.0

Pearson chi2(1) = 39.2645 Pr = 0.000

* The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

Table 22: χ^2 test on *trispondaicus* forms in Gilbert against Bede:^{*}
 . tabi 161 72 \546 295, chi2 expec

Key			
frequency	expected frequency		
col			
row	1	2	Total
1	161	72	233
	153.4	79.6	233.0
2	546	295	841
	553.6	287.4	841.0
Total	707	367	1,074
	707.0	367.0	1,074.0

Pearson chi2(1) = 1.4145 Pr = 0.234

Table 23: χ^2 test on metrical forms in Descartes and Polydore against Bede:^{*}
 . tabi 1430 276 \570 91, chi2 expec

Key			
frequency	expected frequency		
col			
row	1	2	Total
1	1,430	276	1,706
	1,441.5	264.5	1,706.0
2	570	91	661
	558.5	102.5	661.0
Total	2,000	367	2,367
	2,000.0	367.0	2,367.0

Pearson chi2(1) = 2.1142 Pr = 0.146

* The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

Table 24: χ^2 test on metrical forms in Cicero against Bede:^{*}
 . tabi 813 276 \187 91, chi2 expec

Key			
frequency	expected frequency		
col			
row	1	2	Total
1	813	276	1,089
	796.6	292.4	1,089.0
2	187	91	278
	203.4	74.6	278.0
Total	1,000	367	1,367
	1,000.0	367.0	1,367.0

Pearson chi2(1) = 6.1574 Pr = 0.013

0.013×4=0.052 P> α

Table 25: χ^2 test on metrical forms in Dante and John against Bede:^{*}
 . tabi 453 276 \100 91, chi2 expec

Key			
frequency	expected frequency		
col			
row	1	2	Total
1	453	276	729
	438.2	290.8	729.0
2	100	91	191
	114.8	76.2	191.0
Total	553	367	920
	553.0	367.0	920.0

Pearson chi2(1) = 6.0420 Pr = 0.014

0.014×4=0.056 P> α

* The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

Table 26: χ^2 test on metrical forms in Gilbert against Bede:^{*}
 . tabi 579 276 \128 91, chi2 expec

Key			
frequency			
expected frequency			
col			
row	1	2	Total
1	579	276	855
	562.8	292.2	855.0
2	128	91	219
	144.2	74.8	219.0
Total	707	367	1,074
	707.0	367.0	1,074.0

Pearson chi2(1) = 6.6628 Pr = 0.010
 $0.010 \times 4 = 0.04$ P < α

Table 27: forms of final cadence in Bede:

	I	p	$\frac{p}{p}$
6p	0	2	3
5p	0	5	1
5p	1	2	0
p			
4p	3	39	14
4p	1	61	11
p			
3p	5	94	31
3p	3	20	12
p			
2	17	9	24
1	0	9	0

Table 28: expected forms of final cadence for Bede, calculated according to Janson's method:

	I	p	$\frac{p}{p}$
4p	4	37	15
4pp	6	48	19
3p	11	85	34
3pp	3	23	9

* The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

2	4	33	13
other	2	15	6

Table 29: χ^2 test on observed and expected cadence forms in Bede, using Janson's method of internal comparison:

forms	o	e	(o-e)^2/e		pvalue		
14p	3	4.577657	0.543728		0.460892		
14pp	1	5.967302	4.134882		0.042008	0.756144	
13p	5	10.6267	2.979267		0.084337	1.518075	
13pp	3	2.861035	0.00675		0.934522		
"12"	17	4.087193	40.79586		1.69E-10	3.04E-09	sig
1 other	1	1.880109	0.411993		0.52096		
p4p	39	36.77384	0.134764		0.713543		
p4pp	61	47.93733	3.559509		0.059205	1.065695	
p3p	94	85.36785	0.872859		0.350165		
p3pp	20	22.98365	0.387326		0.533708		
p2	9	32.83379	17.30076		3.19E-05	0.000574	sig
p other	18	15.10354	0.555464		0.456094		
pp4p	14	14.6485	0.02871		0.865451		
pp4pp	11	19.09537	3.431983		0.063945		
pp3p	31	34.00545	0.265626		0.606281		
pp3pp	12	9.155313	0.883885		0.34714		
pp2	24	13.07902	9.119019		0.00253	0.045534	sig
pp other	4	6.016349	0.675769		0.411047		
total	367	367					

Equation 3McNemars' test:⁶

$$\chi^2 = \left\{ \frac{|p_2 - p_1| - 1/n}{\text{s.e.}(p_2 - p_1)} \right\}^2 = \frac{(|b - c| - 1)^2}{b + c}$$

$$\text{where } p_1 = \frac{a + c}{n} \text{ and } p_2 = \frac{a + b}{n}$$

from a table:

	Factor Present	Factor Absent	Totals
Factor Present	a	b	a+b
Factor Absent	c	d	c+d
Totals	a+c	b+d	n

⁶ Fleiss, *Statistical Methods*, pp. 113-114.

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Table 30: McNemar's test on the proportion of *14p* cadences in Bede:^{*}
 . symmi 3 53 \27 284, contrib

col			
row	1	2	Total
1	3	53	56
2	27	284	311
Total	30	337	367

Contribution to symmetry Cells	chi-squared
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n1_2 & n2_1 8.4500

	chi2	df	Prob>chi2
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Symmetry (asymptotic) 8.45 1 0.0037

Marginal homogeneity (Stuart-Maxwell) 8.45 1 0.0037

Revised probability: $0.0037 \times 18 = 0.0666$ – therefore slightly over the alpha-boundary of 0.05.

Table 31: McNemar's test on *14pp* cadences in Bede:^{*}
 . symmi 1 72 \29 265, contrib

col			
row	1	2	Total
1	1	72	73
2	29	265	294

Total 30 337 367

Contribution to symmetry Cells	chi-squared
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n1_2 & n2_1 18.3069

	chi2	df	Prob>chi2
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Symmetry (asymptotic) 18.31 1 0.0000

* The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command

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Marginal homogeneity (Stuart-Maxwell) 18.31 1 0.0000

Table 32: McNemar's test on *13p* cadences in Bede:^{*}
. symmi 5 125 \25 212, contrib

col				
row	1	2	Total	
1	5	125	130	
2	25	212	237	
Total	30	337	367	

Contribution to symmetry Cells	chi-squared		
n1_2 & n2_1	66.6667		
		chi2	df
Symmetry (asymptotic)	66.67	1	0.0000
Marginal homogeneity (Stuart-Maxwell)	66.67	1	0.0000

Table 33: McNemar's test on *13pp* cadences in Bede:^{*}
. symmi 3 32 \27 305, contrib

col				
row	1	2	Total	
1	3	32	35	
2	27	305	332	
Total	30	337	367	

Contribution to symmetry Cells	chi-squared		
n1_2 & n2_1	0.4237		
		chi2	df
			Prob>chi2

* The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

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Symmetry (asymptotic)	0.42	1	0.5151
Marginal homogeneity (Stuart-Maxwell)	0.42	1	0.5151
P> α			

Table 34: McNemar's test on *I 2* cadences in Bede:^{*}
 . symmi 17 33 \13 304, contrib

col			
row	1	2	Total
1	17	33	50
2	13	304	317
Total	30	337	367

Contribution			
to symmetry			
Cells	chi-squared		

n1_2 & n2_1	8.6957		

	chi2	df	Prob>chi2
Symmetry (asymptotic)	8.70	1	0.0032
Marginal homogeneity (Stuart-Maxwell)	8.70	1	0.0032
0.0032 × 18 = 0.0576 P> α			

Table 35: McNemar's test on *I other* cadences in Bede:^{*}
 . symmi 1 22 \29 315, contrib

col			
row	1	2	Total
1	1	22	23
2	29	315	344
Total	30	337	367

Contribution			
to symmetry			
Cells	chi-squared		

n1_2 & n2_1	0.9608		

chi2	df	Prob>chi2
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^{*} The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command

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Symmetry (asymptotic)	0.96	1	0.3270
Marginal homogeneity (Stuart-Maxwell)	0.96	1	0.3270
$P > \alpha$			

Table 36: McNemar's test on *p4p* cadences in Bede:^{*}
. symmi 39 17 \202 109, contrib

col			
row	1	2	Total
1	39	17	56
2	202	109	311
Total	241	126	367

Contribution to symmetry Cells	chi-squared	chi2	df	Prob>chi2
n1_2 & n2_1	156.2785			
Symmetry (asymptotic)		156.28	1	0.0000
Marginal homogeneity (Stuart-Maxwell)		156.28	1	0.0000

Table 37: McNemar's test on *p4pp* cadences in Bede:^{*}
. symmi 61 12 \180 114, contrib

col			
row	1	2	Total
1	61	12	73
2	180	114	294
Total	241	126	367

Contribution to symmetry Cells	chi-squared	chi2	df	Prob>chi2
n1_2 & n2_1	147.0000			

^{*} The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

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Symmetry (asymptotic)	147.00	1	0.0000
Marginal homogeneity (Stuart-Maxwell)	147.00	1	0.0000

Table 38: McNemar's test on *p3p* cadences in Bede:^{*}
 . symmi 94 36 \147 90, contrib

col			
row	1	2	Total
1	94	36	130
2	147	90	237
Total	241	126	367

Contribution to symmetry Cells	chi-squared		
<hr/>			
n1_2 & n2_1	67.3279		
		chi2	df
			Prob>chi2
Symmetry (asymptotic)	67.33	1	0.0000
Marginal homogeneity (Stuart-Maxwell)	67.33	1	0.0000

Table 39: McNemar's test on *p3pp* cadences in Bede:^{*}
 . symmi 20 15 \221 111, contrib

col			
row	1	2	Total
1	20	15	35
2	221	111	332
Total	241	126	367

Contribution to symmetry Cells	chi-squared		
<hr/>			
n1_2 & n2_1	179.8136		
		chi2	df
			Prob>chi2
Symmetry (asymptotic)	179.81	1	0.0000
Marginal homogeneity (Stuart-Maxwell)	179.81	1	0.0000

* The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

Table 40: McNemar's test on *p2* cadences in Bede:^{*}
 . symmi 9 41 \232 85, contrib

	col		Total
row	1	2	
1	9	41	50
2	232	85	317
Total	241	126	367

Contribution to symmetry Cells	chi-squared
<hr/>	
n1_2 & n2_1	133.6300

	chi2	df	Prob>chi2
Symmetry (asymptotic)	133.63	1	0.0000
Marginal homogeneity (Stuart-Maxwell)	133.63	1	0.0000

Table 41: McNemar's test on *p other* cadences in Bede:^{*}
 . symmi 18 5 \223 121, contrib

	col		Total
row	1	2	
1	18	5	23
2	223	121	344
Total	241	126	367

Contribution to symmetry Cells	chi-squared
<hr/>	
n1_2 & n2_1	208.4386

	chi2	df	Prob>chi2

* The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

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Symmetry (asymptotic)	208.44	1	0.0000
Marginal homogeneity (Stuart-Maxwell)	208.44	1	0.0000

Table 42: McNemar's test on *pp4p* cadences in Bede:^{*}
 . symmi 14 42 \82 229, contrib

col			
row	1	2	Total
1	14	42	56
2	82	229	311
Total	96	271	367

Contribution to symmetry Cells	chi-squared	chi2	df	Prob>chi2
n1_2 & n2_1	12.9032			
Symmetry (asymptotic)	12.90	1	0.0003	
Marginal homogeneity (Stuart-Maxwell)	12.90	1	0.0003	
0.0003 × 18 = 0.0054	P<α			

Table 43: McNemar's test on *pp4pp* cadences in Bede:^{*}
 . symmi 11 62 \85 269, contrib

col			
row	1	2	Total
1	11	62	73
2	85	269	354
Total	96	331	427

Contribution to symmetry Cells	chi-squared	chi2	df	Prob>chi2
n1_2 & n2_1	3.5986			

* The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

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Symmetry (asymptotic)	3.60	1	0.0578
Marginal homogeneity (Stuart-Maxwell)	3.60	1	0.0578
$0.0478 \times 18 = 0.9$ P> α			

Table 44: McNemar's test on *pp3p* cadences in Bede:^{*}
 . symmi 31 99 \65 172, contrib

col			
row	1	2	Total
1	31	99	130
2	65	172	237
Total	96	271	367

Contribution to symmetry			
Cells	chi-squared		
n1_2 & n2_1	7.0488		

	chi2	df	Prob>chi2
Symmetry (asymptotic)	7.05	1	0.0079
Marginal homogeneity (Stuart-Maxwell)	7.05	1	0.0079
$0.0079 \times 15 = 0.1185$, P> α			

Table 45: McNemar's test on *pp3pp* cadences in Bede:^{*}
 . symmi 12 23 \84 248, contrib

col			
row	1	2	Total
1	12	23	35
2	84	248	332
Total	96	271	367

Contribution to symmetry			
Cells	chi-squared		
n1_2 & n2_1	34.7757		

chi2	df	Prob>chi2
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^{*} The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

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Symmetry (asymptotic)	34.78	1	0.0000
Marginal homogeneity (Stuart-Maxwell)	34.78	1	0.0000

Table 46: McNemar's test on *pp2* cadences in Bede:^{*}
 . symmi 24 26 \72 245, contrib

col			
row	1	2	Total
1	24	26	50
2	72	245	317
Total	96	271	367

Contribution to symmetry Cells	chi-squared	chi2	df	Prob>chi2
n1_2 & n2_1	21.5918			
Symmetry (asymptotic)	21.59	1	0.0000	
Marginal homogeneity (Stuart-Maxwell)	21.59	1	0.0000	

Table 47: McNemar's test on *pp other* cadences in Bede:^{*}
 . symmi 4 19 \92 252, contrib (pp other)

col			
row	1	2	Total
1	4	19	23
2	92	252	344
Total	96	271	367

Contribution to symmetry Cells	chi-squared	chi2	df	Prob>chi2
n1_2 & n2_1	48.0090			

^{*} The values in this table were calculated using the statistical software package Stata 8.0, (©Statacorp, 2003). The first line is the relevant command.

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Symmetry (asymptotic)	48.01	1	0.0000
Marginal homogeneity (Stuart-Maxwell)	48.01	1	0.0000